

UNIT 4 REVIEW - Operations with Polynomials

I. Multiple Choice. Simplify each expression.

1)  $(13p^2 - 1 - 10p^4) - (6p^2 - 4p^3 - 14)$

~~A)  $p^4 + 4p^3 + 7p^2 + 26$~~

B)  $-10p^4 + 4p^3 + 7p^2 + 27$

C)  $-10p^4 + 4p^3 + 7p^2 + 13$

D)  $-10p^4 + 4p^3 + 7p^2 + 26$

$7p^2$   
 $13$   
 $-10p^4$   
 $+4p^3$

2)  $(-8n^2 - 5 - 13n^3) + (-8n^3 - 2n^2 - 2)$

A)  $-21n^3 - 10n^2 - 7$

~~B)  $-21n^3 - 18n^2 + 3$~~

C)  $-21n^3 - 10n^2 + 6$

D)  $-21n^3 - 10n^2 + 3$

$-21n^3$   
 $-10n^2$   
 $-7$

3)  $(7x - 3)(3x + 7)$

A)  $5x^2 + 19x + 12$

B)  $14x^2 - 40$

C)  $21x^2 + 40x - 21$

D)  $14x^2 + 19x - 40$

$21x^2 + 49x - 9x - 21$   
 $21x^2 + 40x - 21$

4)  $7\sqrt{45x^4y^3z^2}$

A)  $30z^2x\sqrt{3xy}$

B)  $21x^2yz\sqrt{5y}$

C)  $27y^2x\sqrt{3xyz}$

D)  $-70x^2\sqrt{10xyz}$

$\sqrt{9x^4y^2z^2} \cdot \sqrt{5y}$   
 $21x^2yz\sqrt{5y}$

5)  $\frac{2\sqrt{3}}{4\sqrt{5}}$

A)  $\frac{\sqrt{3}}{10}$

C) 2

$\frac{\sqrt{3}}{10}$

B)  $\frac{10\sqrt{3}}{3}$

D)  $\frac{\sqrt{6}}{20}$

6)  $-2\sqrt{72} - 2\sqrt{2} + 4\sqrt{8} - 3\sqrt{8}$

A)  $-12\sqrt{2}$

C)  $-18\sqrt{2}$

B)  $-4\sqrt{2}$

D)  $-10\sqrt{2}$

$-12\sqrt{2} - 2\sqrt{2} + 8\sqrt{2} - 6\sqrt{2}$   
 $-14\sqrt{2} + 2\sqrt{2}$   
 $-12\sqrt{2}$

7)  $\frac{4\sqrt{2}}{2-\sqrt{3}} \cdot \frac{2+\sqrt{3}}{2+\sqrt{3}} = \frac{8\sqrt{2} + 4\sqrt{6}}{4-3} = 8\sqrt{2} + 4\sqrt{6}$

A)  $\frac{2+\sqrt{3}}{3}$

C)  $\frac{5+\sqrt{5}}{10}$

B)  $\frac{-2\sqrt{3}-8}{13}$

D)  $8\sqrt{2} + 4\sqrt{6}$

8)  $\frac{-8-5i}{-7+i} \cdot \frac{-7-i}{-7-i} = \frac{56+8i+35i+5i^2}{49-i^2} = \frac{51+43i}{49+1}$

~~A)  $\frac{39+31i}{17}$~~

C)  $\frac{49+7i}{50}$

B)  $\frac{91+13i}{50}$

D)  $\frac{51+43i}{50}$

II. Factor each expression completely.

9)  $48mn + 30m + 64n + 40$

$6m(8n+5) + 8(8n+5)$

$(6m+8)(8n+5)$

$2(3m+4)(8n+5)$

10)  $125 + 216u^3$

Sum of cubes

$\downarrow \quad \downarrow$   
 $5 \quad 6u$

$(5+6u)(25-30u+36u^2)$

$$11) u^4 + u^2 = u^2(u^2 + 1)$$

$$12) a^4 + 7a^2 + 10 = (a^2 + 5)(a^2 + 2)$$

$$13) 6u^8 + 60u^4 + 96$$

$$6(u^8 + 10u^4 + 16)$$

$$6(u^4 + 8)(u^4 + 2)$$

$$14) 4n^2 - 1 = (2n+1)(2n-1)$$

$$15) 3x^4 + 7x^3 - 40x^2$$

$$x^2(3x^2 + 7x - 40)$$

$$x^2(3x - 8)(x + 5)$$

III. Simplify.

$$16) -4\sqrt[3]{147x^2y^2z^5}$$

$$-28xyz^2\sqrt[3]{3z}$$

$$17) \frac{\sqrt{2}-4}{5-\sqrt{2}} \cdot \frac{5+\sqrt{2}}{5+\sqrt{2}} = \frac{5\sqrt{2}+2}{25-2} = \frac{\sqrt{2}-18}{23}$$

$$18) (\sqrt{3} + \sqrt{5})(\sqrt{3} + \sqrt{2})$$

$$3 + \sqrt{6} + \sqrt{15} + \sqrt{10}$$

$$19) (-5 + \sqrt{2})(-1 + \sqrt{2})$$

$$5 - 5\sqrt{2} - \sqrt{2} + 2 = 7 - 6\sqrt{2}$$

$$20) (-7 + 2i)^2(-7 + 2i)$$

$$49 - 28i - 4 = 45 - 28i$$

$$21) i^{-6} = \frac{1}{i^6} = \frac{1}{-1} = -1$$

$$i^2 = -1$$

IV. Quadratics

$$D = b^2 - 4ac$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Find the discriminant of each quadratic equation then state the number and type of solutions.

$$22) 2m^2 - 4m + 2 = 0 \quad D = 16 - 4(2)(2) = 0$$

1 real solution

$$23) 8v^2 - 6v - 3 = -8$$

$$8v^2 - 6v + 5 = 0 \quad D = 36 - 4(8)(5) = 36 - 160 = -124$$

2 imaginary solutions

Solve each equation with the quadratic formula.

$$24) 2v^2 + 3v - 9 = 0$$

$$a=2, b=3, c=-9$$

$$v = \frac{-3 \pm \sqrt{9 - 4(2)(-9)}}{4} = \frac{-3 \pm 9}{4}$$

$$25) 7m^2 = -8m - 5$$

$$7m^2 + 8m + 5 = 0$$

$$m = \frac{-8 \pm \sqrt{64 - 4(7)(5)}}{14}$$

$$= \frac{-8 \pm \sqrt{-76}}{14}$$

$$= \frac{-8 \pm 2i\sqrt{19}}{14} = \frac{-4 \pm i\sqrt{19}}{7}$$

$$v = \frac{-3 \pm \sqrt{9+72}}{4}$$

$$v = \frac{-3 \pm \sqrt{81}}{4}$$

$$\frac{-3+9}{4} = \frac{6}{4} = \frac{3}{2}$$

$$\frac{-3-9}{4} = \frac{-12}{4} = -3$$

$\left\{ \frac{3}{2}, -3 \right\}$