

Released Form

Student Name: _____

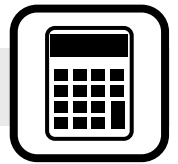
Spring 2013
North Carolina
Measures of Student Learning:
NC's Common Exams
Common Core Math III



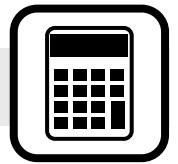
Student Booklet



Public Schools of North Carolina
State Board of Education
Department of Public Instruction
Raleigh, North Carolina 27699-6314



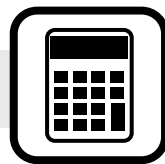
- 1 Which expression is equivalent to $(x + 3)^3 - 9x(x + 3)$?
- A $x^3 + 27$
- B $x^3 - 27$
- C $x^3 - 9x^2 - 27x + 27$
- D $x^3 - 9x^2 + 27x + 27$
- 2 Suppose $p(x) = x^3 - 2x^2 + 13x + k$. The remainder of the division of $p(x)$ by $(x + 1)$ is -8 . What is the remainder of the division of $p(x)$ by $(x - 1)$?
- A -8
- B 8
- C 16
- D 20
- 3 What is the **approximate** solution to the equation $3^{x-1} = 4^{2x+5}$?
- A 3.875
- B 1.262
- C -2.354
- D -4.797



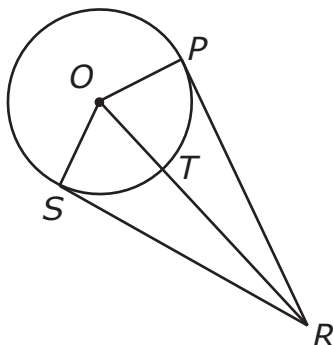
- 4 Samantha invested \$10,000 in each of two different financial plans in 2013. The predicted value of each plan is modeled below.
- Plan M: a rate of 7.5%, compounded continuously.
 - Plan N: The value is determined by the function $y = 5x^3 - 50x^2 + 4x + 10,000$, where x is the number of years after 2013.

Plan N has a greater predicted value than Plan M during which years?

- A from 2014 to 2041
- B from 2028 to 2055
- C from 2042 to 2073
- D Plan N never has a greater value than Plan M.
- 5 Which is an equation of a parabola that has a directrix of $y = -5$ and a focus at $(2, -1)$?
- A $y = \frac{1}{2}(x + 2)^2 + 2$
- B $y = \frac{1}{8}(x + 2)^2 + 3$
- C $y = \frac{1}{8}(x - 2)^2 - 3$
- D $y = \frac{1}{2}(x - 2)^2 - 2$



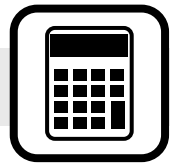
- 6 In the figure below, \overline{PR} and \overline{SR} are tangent to circle O .



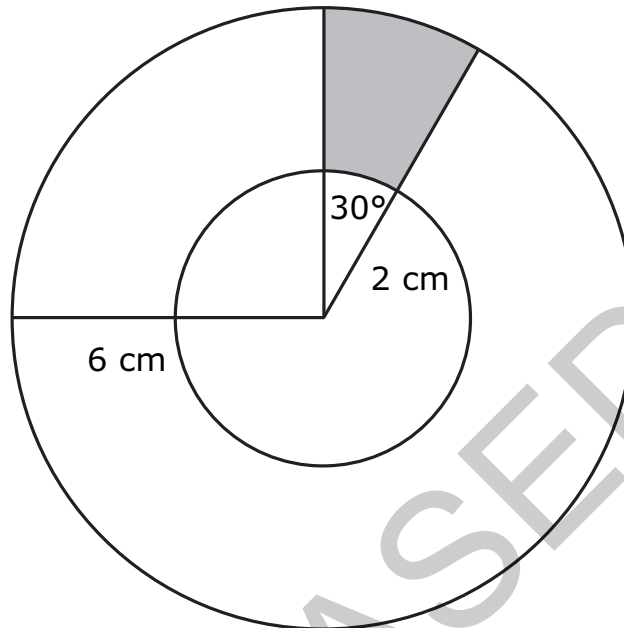
If $OT = 11$ cm and $PR = 60$ cm, what is the length of \overline{OR} ?

- A 61 cm
- B 59 cm
- C 50 cm
- D 48 cm

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- 7 In the figure below, the larger circle has a radius of 6 cm, and the smaller circle has a radius of 2 cm.



What is the **approximate** area of the shaded region?

- A 2.1 cm²
- B 3.4 cm²
- C 4.2 cm²
- D 8.4 cm²



8 Which choice shows the solutions to the equation $8x^2 + 3x = -7$?

A $\frac{-3 \pm i\sqrt{215}}{16}$

B $\frac{3 \pm i\sqrt{215}}{16}$

C $\frac{-3 \pm \sqrt{233}}{16}$

D $\frac{3 \pm \sqrt{233}}{16}$

9 A system of equations is shown below.

$$y = |x - 3|$$

$$y = \frac{1}{2}x$$

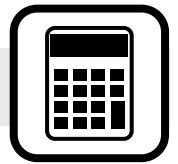
What is the distance between the points of intersection of the system?

A $\sqrt{6}$

B $\sqrt{20}$

C $\sqrt{48}$

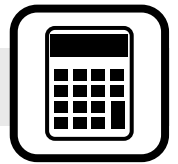
D $\sqrt{80}$



- 10 Fred drives an average of 15,000 miles per year, and his car gets 20 miles per gallon of gasoline.
- The average cost of gasoline is \$3.25 per gallon.
 - He buys a new car.
 - In his new car, Fred continues to average 15,000 miles per year, and the average cost of gasoline remains the same.

Approximately how many more miles per gallon does the new car get if Fred has a savings of \$650 per year on gasoline?

- A 5.8 mpg
- B 7.3 mpg
- C 8.8 mpg
- D 10.3 mpg
- 11 A student wants to determine the most liked professor at her college. Which type of study would be the **most** practical to obtain this information?
- A a simulation
- B an experiment
- C a survey
- D an observation



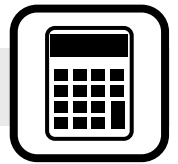
- 12 A principal wants to survey 150 students to determine which electives to offer during the next school year. There are 1,800 students in the school. Which procedure could the principal use to select a sample using a systematic random sample?
- A Obtain a list of all students. Start with the eighth student, and select every twelfth student until 150 students have been selected.
 - B Select the first 150 students who enter the school.
 - C Choose the fifth student to come into the cafeteria, and then select every third student who comes into the cafeteria until 150 students have been selected.
 - D Place students' names on slips of paper and select 150 slips.
- 13 What value of h is needed to complete the square for the equation $x^2 + 10x - 8 = (x - h)^2 - 33$?
- A -25
 - B -5
 - C 5
 - D 25



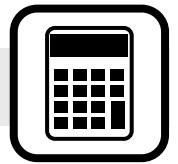
- 14 A shipping company is designing boxes to meet specific requirements.
- Each box must be a completely closed rectangular prism with no overlapping material.
 - The boxes must hold 24 cans in two layers of 12 cans each.
 - The cans are 3 inches in diameter and 5 inches in height.

What is the smallest amount of cardboard needed to meet the specifications?

- A 1,080 in.²
- B 840 in.²
- C 636 in.²
- D 540 in.²
- 15 Which expression is equivalent to $\frac{\cos(\theta)}{1 - \sin(\theta)} - \tan(\theta)$?
- A $\sec(\theta)$
- B $\sin(\theta)$
- C $\cos(\theta)$
- D $\csc(\theta)$



- 16 William put the tip of his pencil on the outer edge of a graph of the unit circle at the point $(0, -1)$. He moved his pencil tip through an angle of $\frac{4\pi}{3}$ radians in the counterclockwise direction along the edge of the circle. At what angle of the unit circle did William's pencil tip stop?
- A $\frac{\pi}{3}$
- B $\frac{5\pi}{6}$
- C $\frac{7\pi}{6}$
- D $\frac{5\pi}{3}$
- 17 A town has 685 households. The number of people per household is normally distributed with a mean, μ , of 3.67 and a standard deviation, σ , of 0.34. **Approximately** how many households have between 2.99 and 4.01 people?
- A 493 households
- B 520 households
- C 558 households
- D 575 households



18 The graph of the function $f(x) = x^3$ will be shifted down 2 units and to the right 3 units. Which is the function that corresponds to the resulting graph?

A $g(x) = (x + 3)^3 + 2$

B $g(x) = (x + 3)^3 - 2$

C $g(x) = (x - 3)^3 + 2$

D $g(x) = (x - 3)^3 - 2$

19 Which is the inverse of $f(x) = 1.5^x + 4$?

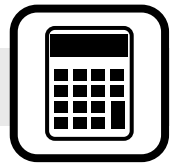
A $f^{-1}(x) = \frac{x - 4}{1.5}$

B $f^{-1}(x) = \frac{\log(x) - 4}{1.5}$

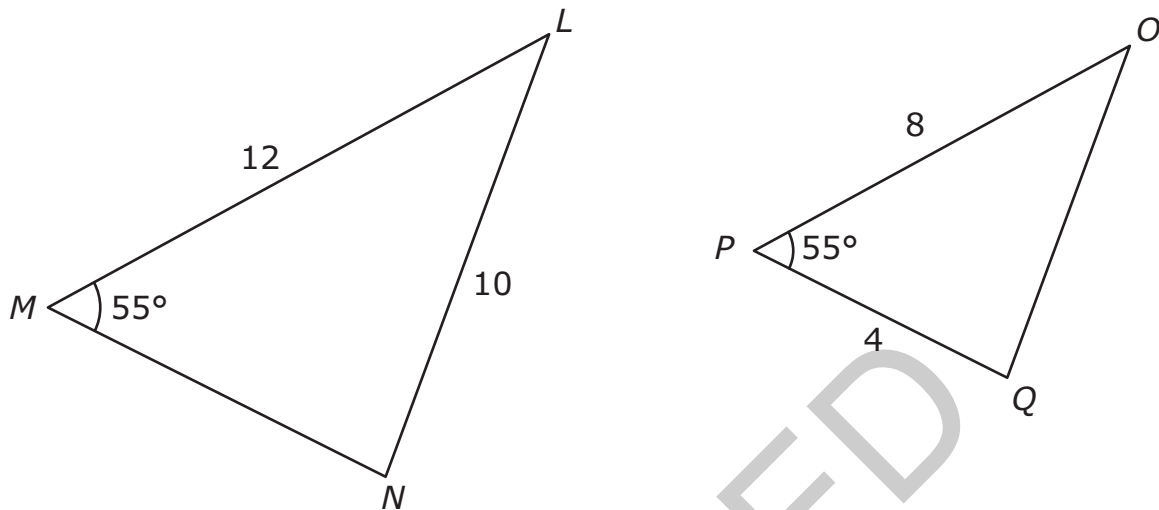
C $f^{-1}(x) = \frac{\log(x - 4)}{\log(1.5)}$

D $f^{-1}(x) = \frac{4 - \log(x)}{\log(1.5)}$

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20 Triangles LMN and OPQ are shown below.



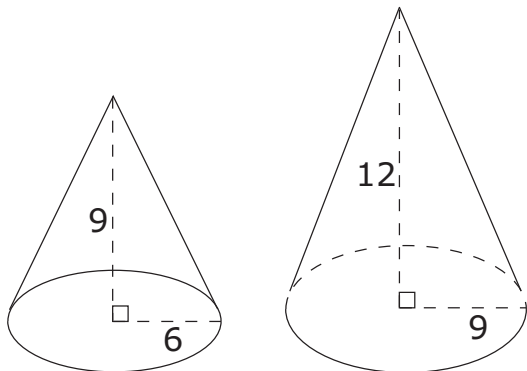
What additional information is sufficient to show that $\triangle LMN$ can be transformed and mapped onto $\triangle OPQ$?

- A $OQ = 6$
- B $MN = 9$
- C $\angle LMN \cong \angle QOP$
- D $\angle NLM \cong \angle QOP$

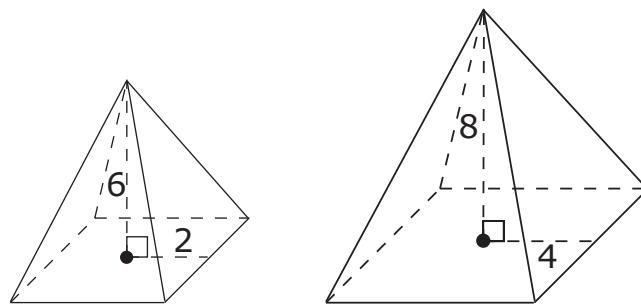


21 Which choice shows a pair of similar figures?

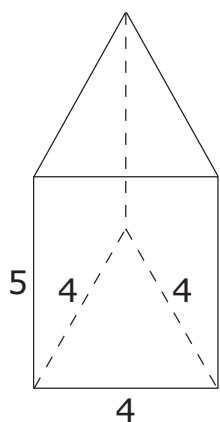
A



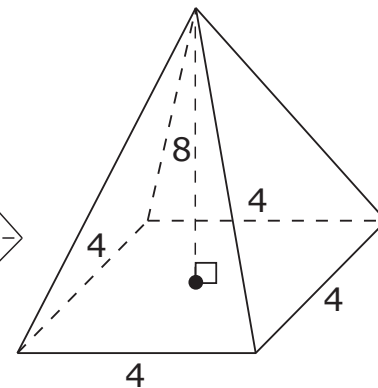
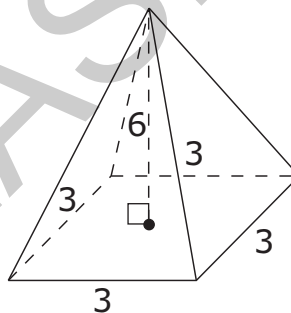
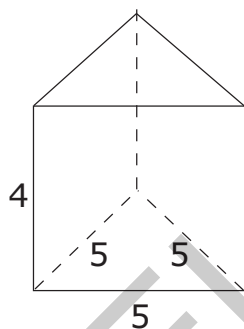
B



C



D

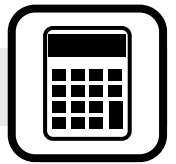


22 What is the **approximate** value of the sum:

$$8 - \frac{8}{7} + \frac{8}{49} - \dots + 8 \cdot \left(-\frac{1}{7}\right)^{2,500} ?$$

(Note: The sum of a series can be calculated using the formula $S_n = \frac{a_1(1 - r^n)}{1 - r}$, where $r \neq 1$.)

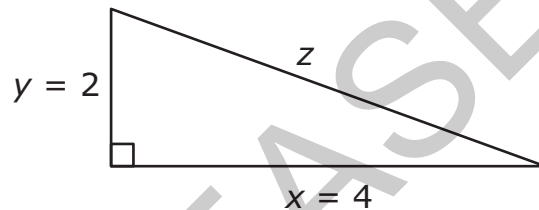
- A 1
- B 7
- C 8
- D 9



- 23 The volume of a rectangular prism is represented by the expression $(x^3 - 2x^2 - 20x - 24)$. If the length is $(x - 6)$ and the height and width are equal, what is the width of the prism?

- A $x + 2$
- B $x - 2$
- C $x + 4$
- D $x - 4$

- 24 A right triangle is shown below.



Which expression would result in an irrational number?

- A $x^2 + y^2$
- B $\frac{1}{2}xy$
- C $x + y + z$
- D $x^2 - z^2$

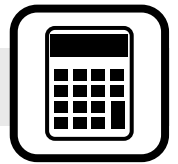


25 Which expression is equivalent to $(4 - 3i)^2 + (6 + i)^2$?

- A 30
- B $42 - 12i$
- C 50
- D $62 - 12i$

This is the end of the multiple-choice portion of the test.

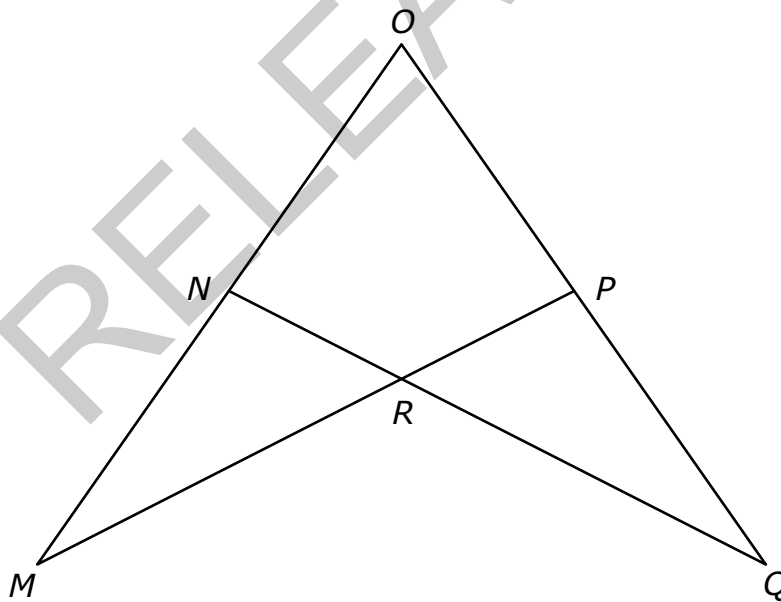
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The questions you read next will require you to answer in writing.

1. Write your answers on separate paper.
2. Be sure to write your name on each page.

- 1 The function f is defined as $f(x) = 6x^4 + x^3 + 4x^2 + x - 2$.
- Using the Remainder Theorem, determine if $\frac{1}{2}$ is a root of $f(x)$. Explain.
 - If i is also a root, what are the other two roots?
- 2 In the diagram of $\triangle OMP$ and $\triangle OQN$, $\angle M \cong \angle Q$ and $\overline{MO} \cong \overline{QO}$.



Based on the diagram, write a proof showing $\overline{MN} \cong \overline{QP}$.



3 Given the function:

$$g(x) = \frac{(x - 2)(3x + 2)}{(x + 4)(x - 2)(x - 6)}$$

- What are the equations of the asymptotes of the function?
- Determine if there are any points of discontinuity. Explain why or why not.
- Describe the end behavior as x approaches $-\infty$ and as x approaches $+\infty$.

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This is the end of the Common Core Math III test.

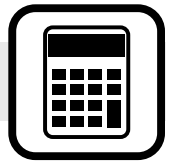
- 1. Look back over your answers.**
- 2. Put all of your papers inside your test book and close the test book.**
- 3. Place your calculator on top of the test book.**
- 4. Stay quietly in your seat until your teacher tells you that testing is finished.**

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Common Core Math III
RELEASED Form
Spring 2013
Answer Key

Item number	Type	Key	Conceptual Category
1	MC	A	A — Algebra
2	MC	D	A — Algebra
3	MC	D	F — Function
4	MC	C	F — Function
5	MC	C	G — Geometry
6	MC	A	G — Geometry
7	MC	D	G — Geometry
8	MC	A	A — Algebra
9	MC	B	A — Algebra
10	MC	B	A — Algebra
11	MC	C	S — Statistics and Probability
12	MC	A	S — Statistics and Probability
13	MC	B	F — Function
14	MC	C	G — Geometry
15	MC	A	F — Function
16	MC	B	F — Function
17	MC	C	S — Statistics and Probability
18	MC	D	F — Function
19	MC	C	F — Function
20	MC	D	G — Geometry
21	MC	D	G — Geometry
22	MC	B	A — Algebra
23	MC	A	A — Algebra



Item number	Type	Key	Conceptual Category
24	MC	C	N — Number and Quantity
25	MC	B	N — Number and Quantity
26	CR	Rubric	A — Algebra
27	CR	Rubric	G — Geometry
28	CR	Rubric	F — Function

Item Types:

MC = multiple choice

CR = constructed response

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